

Integration of MACE breeding values into domestic multi-trait test-day model evaluations

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Objective

The objective of this study was to develop practical approach to **integrate** (blend) **information** from Multiple Across Country Evaluation (**MACE**) to Nordic **test-day model**

This is very critical for

- **single-step evaluations**
- utilization of data from **EUROGENOMICS bull genotype exchange**

Nordic test-day model

- Nordic test-day model is a **multi-trait multi-parity** linear mixed effect model
- **9 traits; milk, protein and fat** in first **three lactations**
- Test-day records from **Finland, Denmark and Sweden (DFS)**
- Due to use of **rank reduction** and **covariance functions** **genetic lactation curves** for 9 traits are modelled using **15 random regression coefficients** per animal

Nordic evaluation model, genetic part

- **Breeding value** \mathbf{a}_i is a vector of 15 regression coefficients
- The same \mathbf{a}_i is used for all the traits, only the covariables change

$$\text{var}(\mathbf{a}_i) = \mathbf{I}_{15}$$

- i.e. each BV is independent and are assumed to have same variance

$$y_{i,m1,d} = \dots + C_{m1,d} \mathbf{a}_i + e$$

$$y_{i,m2,d} = \dots + C_{m2,d} \mathbf{a}_i + e$$

$$y_{i,m3,d} = \dots + C_{m3,d} \mathbf{a}_i + e$$

$$y_{i,p1,d} = \dots + C_{p1,d} \mathbf{a}_i + e$$

$$y_{i,p2,d} = \dots + C_{p2,d} \mathbf{a}_i + e$$

$$y_{i,p3,d} = \dots + C_{p3,d} \mathbf{a}_i + e$$

$$y_{i,f1,d} = \dots + C_{f1,d} \mathbf{a}_i + e$$

$$y_{i,f2,d} = \dots + C_{f2,d} \mathbf{a}_i + e$$

$$y_{i,f3,d} = \dots + C_{f3,d} \mathbf{a}_i + e$$

Nordic evaluation model, genetic part

- **Genetic structure** is implemented using covariables C_{td} specific for each observation
- Covariables are varying according to biological trait, lactation and days in milk (DIM)

$$y_{i,m1,d} = \dots + C_{m1,d} a_i + e$$

$$y_{i,m2,d} = \dots + C_{m2,d} a_i + e$$

$$y_{i,m3,d} = \dots + C_{m3,d} a_i + e$$

$$y_{i,p1,d} = \dots + C_{p1,d} a_i + e$$

$$y_{i,p2,d} = \dots + C_{p2,d} a_i + e$$

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$$y_{i,f1,d} = \dots + C_{f1,d} a_i + e$$

$$y_{i,f2,d} = \dots + C_{f2,d} a_i + e$$

$$y_{i,f3,d} = \dots + C_{f3,d} a_i + e$$

For publishing the EBVs are converted to 305d yield

- **305d EBVs** for animal i , trait t and parity p are calculated as sum of genetic lactation curve over days in milk 8 – 312

$$\widehat{EBV}_{itp} = \sum_{d=8}^{312} C_{tpd} \cdot \hat{a}_i$$

- **3 Combined** EBVs are calculated as **weighted sum** of 305d EBVs

$$\begin{aligned} YI_{it}^{DFS} &= 0.30 \widehat{EBV}_{it1} + 0.25 \widehat{EBV}_{it2} + 0.45 \widehat{EBV}_{it3} \\ &= \left(\sum_{d=8}^{312} 0.30 C_{t1d} + 0.25 C_{t2d} + 0.45 C_{t3d} \right) \hat{a}_i = m_t \hat{a}_i \end{aligned}$$

Interbull MACE

- After each official evaluation run YI_{it}^{DFS} and corresponding reliabilities $R2_{it}^{DFS}$ are submitted to Interbull
- After the MACE **Interbull returns**
 YI_{it}^{MACE} and $R2_{it}^{MACE}$ back us
- These MACE EBVs contain all available information for bulls:
 - ours
 - Eurogenomics countries
 - third countries

Choosing bulls to be blended

- We chose **external** bulls with additional information to be blended into our original test-day model.

Require:

$$R2_{it}^{MACE} - R2_{it}^{DFS} > 0.01$$

- Around 28,000 bulls were selected, some of them had daughters with records in DFS evaluation
- To avoid **double counting** Nordic information has to be removed from MACE EBVs before “blending” it to test-day model

Calculating pseudo-observation

- Multi-trait **ERC** and **DRP** for milk, protein and fat were calculated based on **MACE** and **DFS** combined EBVs and reliabilities for each bull ***i***
- Amount of additional information is

$$ERC_{it}^{BL} = ERC_{it}^{MACE} - ERC_{it}^{DFS}$$

- **Pseudo-observation** was calculated as

$$DRP_{it}^{BL} = \frac{ERC_{it}^{MACE} \cdot DRP_{it}^{MACE} - ERC_{it}^{DFS} \cdot DRP_{it}^{DFS}}{ERC_{it}^{MACE} - ERC_{it}^{DFS}}$$

- DRP_{it}^{BL} was included in the model as observation using ERC_{it}^{BL} as weight

Inclusion of pseudo-observations into the Test Day model

- Model for pseudo-observations (**ERCs** as a weight) in test-day model

$$DRP_{i; \text{milk}}^{BL} = \mu_{\text{milk}} + m_{\text{milk}} \mathbf{a}_i$$

$$DRP_{i; \text{prot}}^{BL} = \mu_{\text{prot}} + m_{\text{prot}} \mathbf{a}_i$$

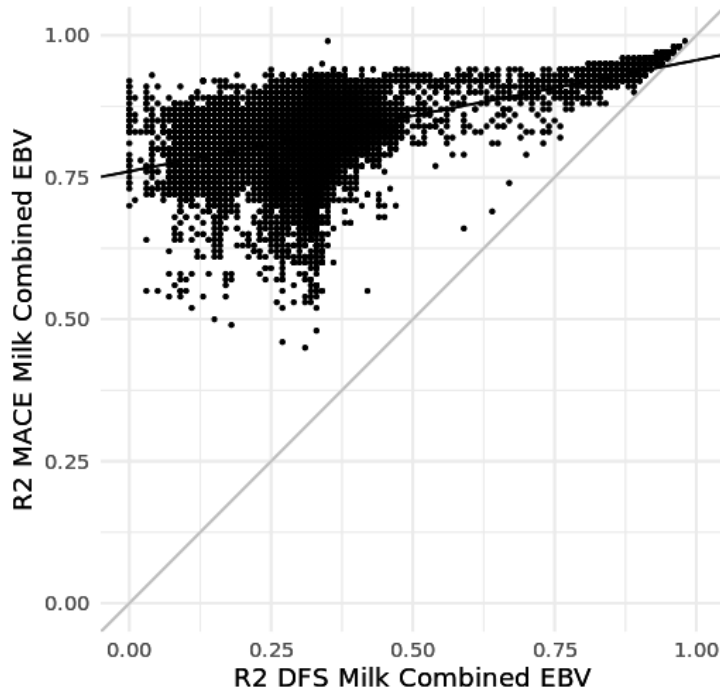
$$DRP_{i; \text{fat}}^{BL} = \mu_{\text{fat}} + m_{\text{fat}} \mathbf{a}_i$$

- NOTE!** The vector \mathbf{a}_i is used also for pseudo-observations!

Results, R2 for combined EBVs

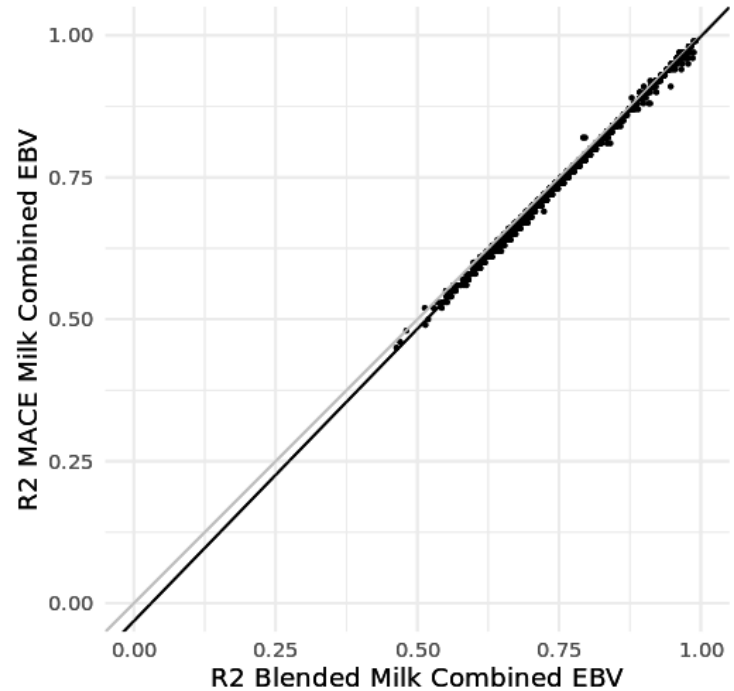
R2 BEFORE BLENDING MILK

$y = 0.76 + 0.196x$ $\text{corr} = 0.45$
 $\text{sd}(Y) = 0.05$ $\text{sd}(x) = 0.12$ $N = 27958$



R2 AFTER BLENDING MILK

$y = -0.03 + 1.029x$ $\text{corr} = 1$
 $\text{sd}(Y) = 0.05$ $\text{sd}(x) = 0.05$ $N = 27958$

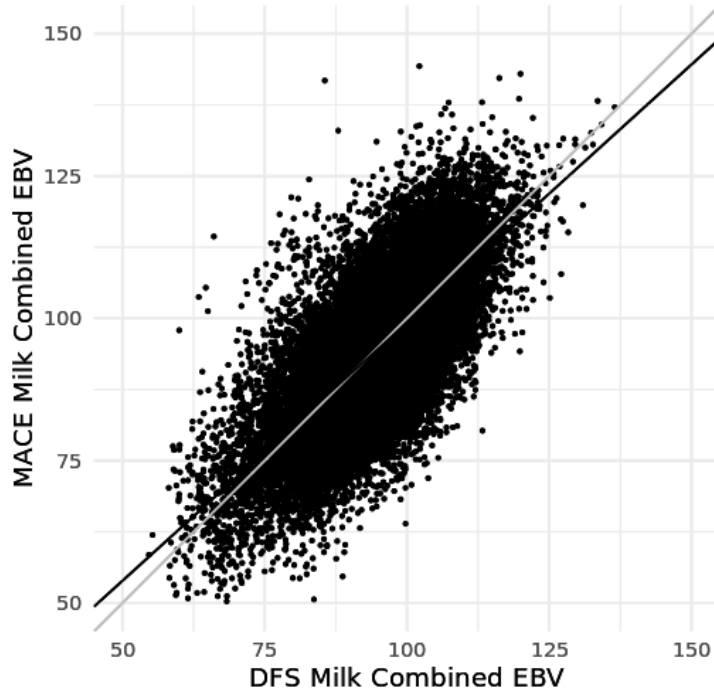


Results, Combined milk EBVs

BEFORE BLENDING MILK

$$y = 8.54 + 0.907x \quad \text{corr} = 0.72$$

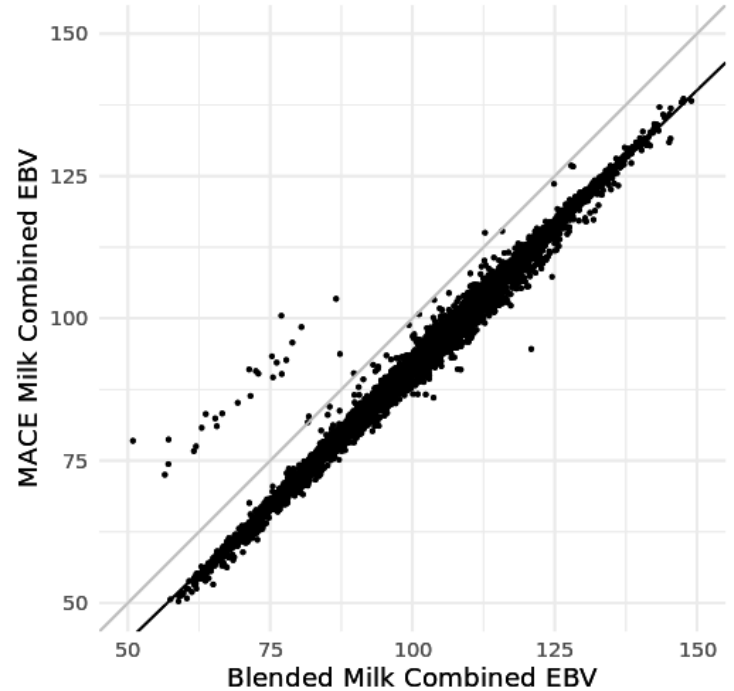
sd(Y) = 12 sd(x) = 10 N = 27958



AFTER BLENDING MILK

$$y = -5.05 + 0.967x \quad \text{corr} = 0.99$$

sd(Y) = 12 sd(x) = 13 N = 27958



Conclusions

- Blending of information from MACE EBVs to test-day model works very well
 - Each pseudo-observation is modelled by all **15 BV coefficients**
- Correlations between MACE and Blended combined EBVs was 0.99 for all three traits
- Also correlations between R2s were > 0.99
- Blending procedure has multiple steps which depend on the evaluation model

Thank you!

